

# Package ‘BNPmix’

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**Description** Performs Bayesian nonparametric univariate and multivariate density estimation and clustering by means of Pitman-Yor mixtures and Dependent Dirichlet process mixtures for partially exchangeable data.

**License** LGPL-3 | file LICENSE

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---

cDDP *C++ function to estimate DDP models with 1 grouping variables*

---

## Description

C++ function to estimate DDP models with 1 grouping variables

## Arguments

data	a vector of observations.
group	group allocation of the data.
ngr	number of groups.
grid	vector to evaluate the density.
niter	number of iterations.
nburn	number of burn-in iterations.
m0	expectation of location component.
k0	tuning parameter of variance of location component.
a0	parameter of scale component.
b0	parameter of scale component.
mass	mass of Dirichlet process.
wei	prior weight of the specific processes.
napprox	number of approximating values.
n_approx_unif	number of approximating values of the importance step for the weights updating.
nupd	number of iterations to show current updating.
out_dens	if TRUE, return also the estimated density (default TRUE).
print_message	print the status.
light_dens	if TRUE return only the posterior mean of the density

## Examples

```
{
  data_toy <- c(rnorm(50, -4, 1), rnorm(100, 0, 1), rnorm(50, 4, 1))
  group_toy <- c(rep(1,100), rep(2,100))
  grid <- seq(-7, 7, length.out = 50)
  est_model <- cDDP(data_toy, group_toy, 2, grid, 20, 10,
    0, 1, 2, 1, 1, 0.5, 10, 1000, 100, 1, 1, 1)
```

```

data_toy <- c(rnorm(50, -4, 1), rnorm(100, 0, 1), rnorm(50, 4, 1))
group_toy <- c(rep(1,100), rep(2,100))
grid <- seq(-7, 7, length.out = 50)
est_model <- cDDP(data_toy, group_toy, 2, grid, 1000, 100,
  0, 1, 2, 1, 1, 0.5, 10, 1000, 100, 1, 1, 1)
}

```

---

cICS

*C++ function to estimate Pitman-Yor univariate mixtures via importance conditional sampler*


---

### Description

C++ function to estimate Pitman-Yor univariate mixtures via importance conditional sampler

### Arguments

data	a vector of observations
grid	vector to evaluate the density
niter	number of iterations
nburn	number of burn-in iterations
m0	expectation of location component
k0	tuning parameter of variance of location component
a0	parameter of scale component
b0	parameter of scale component
mass	mass of Dirichlet process
napprox	number of approximating values
nupd	number of iterations to show current updating
out_param	if TRUE, return also the location and scale parameters lists
out_dens	if TRUE, return also the estimated density (default TRUE)
sigma_PY	second parameter of PY
print_message	print the status

### Examples

```

{
data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))
grid <- seq(-7, 7, length.out = 50)
est_model <- cICS(data_toy, grid, 20, 10, 0, 1, 2, 1, 1, 10, 100, 0, 1, 0, 1)
}

```

```

data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))
grid <- seq(-7, 7, length.out = 50)
est_model <- cICS(data_toy, grid, 1000, 100, 0, 1, 2, 1, 1, 10, 100, 0, 1, 0, 1)

}

```

---

cICS\_mv

*C++ function to estimate Pitman-Yor multivariate mixtures via importance conditional sampler*


---

### Description

C++ function to estimate Pitman-Yor multivariate mixtures via importance conditional sampler

### Arguments

data	a matrix of observations
grid	matrix of points to evaluate the density
niter	number of iterations
nburn	number of burn-in iterations
m0	expectation of location component
k0	tuning parameter of variance of location component
S0	parameter of scale component
n0	parameter of scale component
mass	mass of Dirichlet process
napprox	number of approximating values
nupd	number of iterations to show current updating
out_param	if TRUE, return also the location and scale parameters lists
out_dens	if TRUE, return also the estimated density (default TRUE)
sigma_PY	second parameter of PY
print_message	print the status
light_dens	if TRUE return only the posterior mean of the density

### Examples

```

{
data_toy <- cbind(c(rnorm(100, -3, 1), rnorm(100, 3, 1)),
                c(rnorm(100, -3, 1), rnorm(100, 3, 1)))
grid <- as.matrix(expand.grid(seq(-7, 7, length.out = 50),
                             seq(-7, 7, length.out = 50)))
est_model <- cICS_mv(data_toy, grid, 20, 10,
                    c(0,0), 1, diag(1,2), 4, 1, 100, 100, 0, 1, 0, 1, 1)
}

```

```

data_toy <- cbind(c(rnorm(100, -3, 1), rnorm(100, 3, 1)),
                 c(rnorm(100, -3, 1), rnorm(100, 3, 1)))
grid <- as.matrix(expand.grid(seq(-7, 7, length.out = 50),
                             seq(-7, 7, length.out = 50)))
est_model <- cICS_mv(data_toy, grid, 1000, 100,
                    c(0,0), 1, diag(1,2), 4, 1, 100, 100, 0, 1, 0, 1, 1)
}

```

---

condDDP

*Conditional dependent Dirichlet process*


---

### Description

Conditional dependent Dirichlet process

Estimate an univariate dependent Dirichlet process mixture model with Gaussian kernel using importance conditional sampler scheme.

### Usage

```

condDDP(data, group, grid = NULL, niter, nburn, m0 = NULL, k0 = NULL,
        a0 = NULL, b0 = NULL, mass = 1, wei = 0.5, napprox = 10,
        n_approx_unif = 1000, nupd = 1000, out_dens = TRUE,
        print_message = TRUE, light_dens = FALSE)

```

### Arguments

<code>data</code>	A dataset (vector).
<code>group</code>	group for the observed data, same length as data.
<code>grid</code>	A grid to evaluate the estimated density (vector).
<code>niter</code>	Number of iterations to estimate the model.
<code>nburn</code>	Number of burn-in iterations.
<code>m0</code>	Mean of the location component of the base measure.
<code>k0</code>	Tuning parameter of the variance for the location component of the base measure.
<code>a0</code>	Shape parameter of the scale component of the base measure.
<code>b0</code>	Rate parameter of the scale component of the base measure.
<code>mass</code>	Total mass.
<code>wei</code>	weight of the idiosyncratic process.
<code>napprox</code>	Number of values to be sampled from the restricted process via "ICS" method, default 100.

n_approx_unif	number of values used in the importance sampling step for the multivariate beta distribution.
nupd	How frequently show the current state of the estimation (number of iterations) - default 1000.
out_dens	If TRUE, save the parameters for each iteration, default TRUE.
print_message	Print the status of the estimation.
light_dens	Return only the posterior mean of the densities.

### Value

A modCond class object contain the estimated density for each iterations, the allocations for each iterations. If out\_param is TRUE, also the parameters.

### Examples

```
set.seed(42)
data_toy <- c(rnorm(50, -4, 1), rnorm(100, 0, 1), rnorm(50, 4, 1))
group_toy <- c(rep(1,100), rep(2,100))
grid <- seq(-7, 7, length.out = 50)
est_model <- condDDP(data = data_toy, group = group_toy, grid = grid, niter = 1000,
                    nburn = 100, napprox = 100, nupd = 100)
summary(est_model)
plot(est_model)
```

---

condMCMC

*MCMC for univariate Pitman-Yor mixtures*

---

### Description

The condMCMC function estimate a univariate Pitman-Yor process mixture model with Gaussian kernel. Three possible sampling strategies: importance conditional sampler, slice sampler and marginal sampler.

The models are of the form

$$\tilde{f}(x) = \int k(x; \mu, \sigma^2) \tilde{p}(d\mu, d\sigma^2)$$

where  $k(x; \mu, \sigma^2)$  is an univariate gaussian kernel function,  $\tilde{p}$  is distributed as a Pitman-Yor process with total mass  $\vartheta$ , discount parameter  $\sigma$  and normal-inverse-gamma base measure  $P_0$ , i.e.

$$P_0 \sim N(\mu; m_0, k_0 \sigma^2) \times IG(\sigma^2; a_0, b_0).$$

### Usage

```
condMCMC(data, grid = NULL, niter, nburn, m0 = NULL, k0 = NULL,
         a0 = NULL, b0 = NULL, mass = 1, method = "ICS", napprox = 100,
         nupd = 1000, out_param = F, out_dens = TRUE, process = "DP",
         sigma_PY = 0, print_message = TRUE)
```

**Arguments**

<code>data</code>	A dataset (vector).
<code>grid</code>	A grid of points to evaluate the estimated density (vector).
<code>niter</code>	Number of iterations to estimate the model.
<code>nburn</code>	Number of burn-in iterations.
<code>m0</code>	Mean of the location component of the base measure.
<code>k0</code>	Tuning parameter of the variance for the location component of the base measure.
<code>a0</code>	Shape parameter of the scale component of the base measure.
<code>b0</code>	Rate parameter of the scale component of the base measure.
<code>mass</code>	Mass parameter.
<code>method</code>	Different methods to estimate the model. Possible vaule "ICS", "SLI" or "MAR", importance conditional sampler/slice sampler/marginal sampler, default "ICS".
<code>napprox</code>	Number of values to be sampled from the restricted process via "ICS" method, default 100.
<code>nupd</code>	How frequently show the curren state of the estimation (number of iterations) - default 1000.
<code>out_param</code>	If TRUE, save the parameters for each iteration, default FALSE.
<code>out_dens</code>	If TRUE, return also the estimated density, default TRUE.
<code>process</code>	Dirichlet process ("DP") or Pitman-Yor process ("PY"), default "DP".
<code>sigma_PY</code>	Discount parameter of the Pitman-Yor process, default 0.
<code>print_message</code>	If TRUE print the status of the estimation, default TRUE.

**Value**

A modCond class object contain the estimated density for each iterations, the allocations for each iterations. If `out_param` is TRUE, also the parameters for each iteration.

**Examples**

```
data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))
grid <- seq(-7, 7, length.out = 50)
est_model <- condMCMC(data = data_toy, grid = grid, niter = 1000,
                     nburn = 100, napprox = 100, nupd = 100)
summary(est_model)
plot(est_model)
```

**Description**

The condMCMCmv function estimate a multivariate Pitman-Yor process mixture model with Gaussian kernel. Three possible sampling strategies: importance conditional sampler, slice sampler and marginal sampler.

The models are of the form

$$\tilde{f}(\mathbf{x}) = \int k(\mathbf{x}; \mu, \Sigma) \tilde{p}(d\mu, d\Sigma)$$

where  $k(\mathbf{x}; \mu, \Sigma)$  is a multivariate gaussian kernel function,  $\tilde{p}$  is distributed as a Pitman-Yor process with total mass  $\vartheta$ , discount parameter  $\sigma$  and normal-inverse-wishart base measure  $P_0$ , i.e.

$$P_0 \sim N(\mu; \mathbf{m}_0, k_0 \Sigma) \times IW(\Sigma; n_0, S_0).$$

**Usage**

```
condMCMCmv(data, grid = NULL, niter, nburn, m0 = NULL, k0 = NULL,
  S0 = NULL, n0 = NULL, mass = 1, method = "ICS", napprox = 100,
  nupd = 1000, out_param = F, out_dens = TRUE, process = "DP",
  sigma_PY = 0, print_message = TRUE, light_dens = TRUE)
```

**Arguments**

data	A dataset (matrix).
grid	A grid of points to evaluate the estimated density (matrix).
niter	Number of iterations to estimate the model.
nburn	Number of burn-in iterations.
m0	Mean of location component of the base measure.
k0	Tuning parameter of the variance for the location component of the base measure.
S0	Matrix of the Inverse Wishart distribution of the scale component.
n0	Degree of freedom of the Inverse Wishart distribution of the scale component.
mass	Mass parameter.
method	Different methods to estimate the model. Possible vaule "ICS", "SLI" or "MAR", importance conditional sampler/slice sampler/marginal sampler, default "ICS".
napprox	Number of values to be sampled from the restricted process via "ICS" method, default 100.
nupd	How frequently show the curren state of the estimation (number of iterations) - default 1000.
out_param	If TRUE, save the parameters for each iteration, default FALSE.
out_dens	If TRUE, return also the estimated density, default TRUE.



process	Dirichlet process ("DP") or Pitman-Yor process ("PY"), default "DP".
sigma_PY	Discount parameter of the Pitman-Yor process, default 0.
print_message	If TRUE print the status of the estimation, default TRUE.
light_dens	If TRUE return only the mean of the estimated densities, default TRUE.

**Value**

A modCondMv class object contain the estimated density for each iterations, the allocations for each iterations. If out\_param is TRUE, also the parameters for each iteration.

**Examples**

```
data_toy <- cbind(c(rnorm(100, -3, 1), rnorm(100, 3, 1)),
                 c(rnorm(100, -3, 1), rnorm(100, 3, 1)))
grid <- expand.grid(seq(-7, 7, length.out = 50),
                  seq(-7, 7, length.out = 50))
est_model <- condMCMCmv(data = data_toy, grid = grid, niter = 1000,
                       nburn = 100, napprox = 100, nupd = 100)
summary(est_model)
plot(est_model)
```

---

cSLI	<i>C++ function to estimate Pitman-Yor univariate mixtures via slice sampler</i>
------	--

---

**Description**

C++ function to estimate Pitman-Yor univariate mixtures via slice sampler

**Arguments**

data	a vector of observations
grid	vector to evaluate the density
niter	number of iterations
nburn	number of burn-in iterations
m0	expectation of location component
k0	tuning parameter of variance of location component
a0	parameter of scale component
b0	parameter of scale component
mass	mass of Dirichlet process
nupd	number of iterations to show current updating
out_param	if TRUE, return also the location and scale paramteres lists
out_dens	if TRUE, return also the estimated density (default TRUE)
sigma_PY	second parameter of PY
print_message	print the status

**Examples**

```

{
  data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))
  grid <- seq(-7, 7, length.out = 50)
  est_model <- cSLI(data_toy, grid, 20, 10, 0, 1, 2, 1, 1, 100, 0, 1, 0, 1)

  data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))
  grid <- seq(-7, 7, length.out = 50)
  est_model <- cSLI(data_toy, grid, 1000, 100, 0, 1, 2, 1, 1, 100, 0, 1, 0, 1)
}

```

cSLI\_mv

*C++ function to estimate Pitman-Yor multivariate mixtures via slice sampler*

**Description**

C++ function to estimate Pitman-Yor multivariate mixtures via slice sampler

**Arguments**

data	a matrix of observations
grid	matrix of points to evaluate the density
niter	number of iterations
nburn	number of burn-in iterations
m0	expectation of location component
k0	tuning parameter of variance of location component
S0	parameter of scale component
n0	parameter of scale component
mass	mass of Dirichlet process
nupd	number of iterations to show current updating
out_param	if TRUE, return also the location and scale parameters lists
out_dens	if TRUE, return also the estimated density (default TRUE)
sigma_PY	second parameter of PY
print_message	print the status
light_dens	if TRUE return only the posterior mean of the density

**Examples**

```

{
  data_toy <- cbind(c(rnorm(100, -3, 1), rnorm(100, 3, 1)),
                  c(rnorm(100, -3, 1), rnorm(100, 3, 1)))
  grid <- as.matrix(expand.grid(seq(-7, 7, length.out = 50),
                               seq(-7, 7, length.out = 50)))
  est_model <- cSLI_mv(data_toy, grid, 20, 10, c(0,0), 1, diag(1,2), 4, 1, 100, 0, 1, 0, 1, 1)

  data_toy <- cbind(c(rnorm(100, -3, 1), rnorm(100, 3, 1)),
                  c(rnorm(100, -3, 1), rnorm(100, 3, 1)))
  grid <- as.matrix(expand.grid(seq(-7, 7, length.out = 50),
                               seq(-7, 7, length.out = 50)))
  est_model <- cSLI_mv(data_toy, grid, 1000, 100, c(0,0), 1, diag(1,2), 4, 1, 100, 0, 1, 0, 1, 1)
}

```

MAR

*C++ function to estimate Pitman-Yor univariate mixtures via marginal sampler*

**Description**

C++ function to estimate Pitman-Yor univariate mixtures via marginal sampler

**Arguments**

data	a vector of observations
grid	vector to evaluate the density
niter	number of iterations
nburn	number of burn-in iterations
m0	expectation of location component
k0	tuning parameter of variance of location component
a0	parameter of scale component
b0	parameter of scale component
mass	mass of Dirichlet process
nupd	number of iterations to show current updating
out_param	if TRUE, return also the location and scale parameters lists
out_dens	if TRUE, return also the estimated density (default TRUE)
process	if 0 DP, if 1 PY
sigma_PY	second parameter of PY
print_message	print the status

**Examples**

```

{
  data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))
  grid <- seq(-7, 7, length.out = 50)
  est_model <- MAR(data_toy, grid, 50, 10, 0, 1, 2, 1, 1, 100, 0, 1, 0, 1)

  data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))
  grid <- seq(-7, 7, length.out = 50)
  est_model <- MAR(data_toy, grid, 1000, 100, 0, 1, 2, 1, 1, 100, 0, 1, 0, 1)
}

```

MAR\_mv

*C++ function to estimate Pitman-Yor multivariate mixtures via marginal sampler*

**Description**

C++ function to estimate Pitman-Yor multivariate mixtures via marginal sampler

**Arguments**

data	a matrix of observations
grid	matrix of points to evaluate the density
niter	number of iterations
nburn	number of burn-in iterations
m0	expectation of location component
k0	tuning parameter of variance of location component
S0	parameter of scale component
n0	parameter of scale component
mass	mass of Dirichlet process
nupd	number of iterations to show current updating
out_param	if TRUE, return also the location and scale parameters lists
out_dens	if TRUE, return also the estimated density (default TRUE)
sigma_PY	second parameter of PY
print_message	print the status
light_dens	if TRUE return only the posterior mean of the density

**Examples**

```

{
  data_toy <- cbind(c(rnorm(100, -3, 1), rnorm(100, 3, 1)),
                  c(rnorm(100, -3, 1), rnorm(100, 3, 1)))
  grid <- as.matrix(expand.grid(seq(-7, 7, length.out = 50),
                               seq(-7, 7, length.out = 50)))
  est_model <- MAR_mv(data_toy, grid, 20, 10, c(0,0), 1, diag(1,2), 4, 1, 100, 0, 1, 0, 1, 1)

  data_toy <- cbind(c(rnorm(100, -3, 1), rnorm(100, 3, 1)),
                  c(rnorm(100, -3, 1), rnorm(100, 3, 1)))
  grid <- as.matrix(expand.grid(seq(-7, 7, length.out = 50),
                               seq(-7, 7, length.out = 50)))
  est_model <- MAR_mv(data_toy, grid, 1000, 100, c(0,0), 1, diag(1,2), 4, 1, 100, 0, 1, 0, 1, 1)
}

```

---

modCond

*modCond class constructor*


---

**Description**

define the modCond class, could be for univariate or multivariate estimated models

**Usage**

```

modCond(density = NULL, grideval = NULL, clust = NULL, mean = NULL,
        sigma2 = NULL, probs = NULL, niter = NULL, nburn = NULL,
        nnew = NULL, tot_time = NULL, univariate = TRUE, dep = FALSE,
        group_log = NULL, nclust = NULL, group = NULL, wvals = NULL)

```

**Arguments**

density	a matrix containing the density value corresponding to the grid points
grideval	a set of values to evaluate the density
clust	a matrix containing the corresponding clusters for each observation, for each iteration
mean	values for the location parameters
sigma2	values for the scale parameters
probs	values for the mixing measure
niter	number of iterations
nburn	number of burn-in iterations
nnew	number of new clusters sampled at each iteration
tot_time	execution time

univariate	if the model is univariate (TRUE/FALSE)
dep	if the model is dependent Dirichlet process (TRUE/FALSE)
group_log	group allocation for dependent Dirichlet process
nclust	number of cluster for dependent Dirichlet process
group	true group allocation for dependent Dirichlet process
wvals	values of the processes weights

### Examples

```
data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))
grid <- seq(-7, 7, length.out = 50)
est_model <- condMCMC(data = data_toy, grid = grid, niter = 1000,
                     nburn = 100, napprox = 100, nupd = 100)
str(est_model)
class(est_model)
```

---

plot.modCond	<i>modCond summary method</i>
--------------	-------------------------------

---

### Description

modCond summary method

### Usage

```
## S3 method for class 'modCond'
plot(x, dimension = c(1, 2), col = "#0037c4", ...)
```

### Arguments

x	an object of class modCond
dimension	if multivariate, the two dimensions for the plot (if they are equal, a marginal plot is performed)
col	the color of the lines
...	additional arguments to be passed

### Examples

```
data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))
grid <- seq(-7, 7, length.out = 50)
est_model <- condMCMC(data = data_toy, grid = grid, niter = 1000,
                     nburn = 100, napprox = 100, nupd = 100)
class(est_model)
plot(est_model)
```

---

summary.modCond	<i>modCond summary method</i>
-----------------	-------------------------------

---

**Description**

modCond summary method

**Usage**

```
## S3 method for class 'modCond'  
summary(object, ...)
```

**Arguments**

object	an object of class modCond
...	additional arguments to be passed

**Examples**

```
data_toy <- c(rnorm(100, -3, 1), rnorm(100, 3, 1))  
grid <- seq(-7, 7, length.out = 50)  
est_model <- condMCMC(data = data_toy, grid = grid, niter = 1000,  
                      nburn = 100, napprox = 100, nupd = 100)  
class(est_model)  
summary(est_model)
```

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